## Warm up

1. Rewrite.
a. $x^{4}=3$
b. $e^{5}=x$
c. $\log _{3} x=7$
d. $\ln x=r$
2. Evaluate
a. $\log _{4} \frac{1}{16}-\log _{3} 81$
b. $4 \ln e^{6}$
3. Solve
$x^{4}-4 x^{2}-12=0$
4. Sketch by hand.
a. $\quad f(x)=e^{x-1}+3$
b. $f(x)=\log (-x)-4$


# 3.4 Solving Equations Day 1 Matching bases <br> Exponential 

## Solve

$$
\begin{aligned}
5^{x} & =125 \\
5^{x} & =5^{3} \\
x & =3
\end{aligned}
$$

$$
\begin{array}{rlr}
\left(\frac{1}{2}\right)^{x}=8 & 9^{x+1}=2 \\
\left(2^{-1}\right)^{x}=8 & \left(3^{2}\right)^{x+1}=3^{3} \\
2^{-x}=2^{3} & 3^{2 x+2}=3^{3} \\
-x=3 & 2 x+2=3 \\
x=-3 & 2 x=1 \\
& x=\frac{1}{2}
\end{array}
$$



$$
\begin{aligned}
& 4+2 e^{3 x}=9 \\
&-4 \\
& \frac{2 e^{3 x}}{2}=\frac{5}{2} \\
& e^{3 x}=\frac{5}{2} \\
& 6\left(2^{4 x-1}\right)-5=19 \\
& \frac{6}{6}\left(2^{4 x-1}\right)=\frac{24}{6} \\
& \frac{2^{4 x-1}}{2}=\frac{4}{3} \\
& 305=x \quad \text { Cant divide by the base } \\
& 2^{4 x-1}=2^{2} \\
& 4 x-1=\frac{3 x}{3} \\
& x=\frac{3}{4}
\end{aligned} \quad \begin{aligned}
\frac{3}{3} \frac{\ln }{2} \\
3
\end{aligned}
$$

$$
\begin{aligned}
& e^{2 x}-4 e^{x}+3=0 \quad \text { quadratic! } \\
& \left(e^{x}\right)^{2}-4 e^{x}+3=0 \quad 3 \Rightarrow-3,-1 \\
& \begin{array}{c}
\left(e^{x}-3\right)\left(e^{x}-1\right) \\
e^{x}=3 \mid e^{x}=1
\end{array} \longrightarrow \begin{array}{c}
\ln 3=x \quad \left\lvert\, \begin{array}{c}
-4 \\
1.1=x
\end{array} \quad \begin{array}{c}
\ln 1=x \\
0=x
\end{array}\right.
\end{array} \\
& 3^{x}=4^{x-1} \\
& \log 3^{x}=\log 4^{x-1} \\
& x \log 3=(x-1)) \log 4 \longrightarrow x=\frac{-\log 4}{\log 3-\log 4} \\
& x \log 3=x \log 4-\underline{\log 4} \\
& x \log 3-x \log 4=-\log 4 \\
& x(\log 3-\log 4)=-\log 4
\end{aligned}
$$

