




GO COUGARS! 

p 292 **Homework Questions**

In Exercises 79-82, find the angle in radians.

79. 

80. 

In Exercises 83-86, find the radian measure of the central angle of a circle of radius r that intercepts an arc of length s .

83. 17 inches, 6 inches

84. 14.5 centimeters, 23 centimeters

In Exercises 87-90, find the length of the arc on a circle of radius r intercepted by a central angle θ .

87. 15 inches, 130°

88. 3 meters, 1.6 radians

In Exercises 91-94, find the area of the sector of the circle with radius r and central angle θ .

91. 4 inches, $\frac{\pi}{2}$


92. 2.5 feet, 225°

Distance Between Cities In Exercises 95 and 96, find the distance between the cities. Assume that Earth is a sphere of radius 4000 miles and that the cities are in the same hemisphere (over city is due north of the other).

95. Dallas, Texas, $32^\circ 47' 39''$ N
 Omaha, Nebraska, $41^\circ 15' 50''$ N

96. Difference in Latitude Assuming that Earth is a sphere of radius 4000 kilometers, what is the difference in the latitudes of Toronto, New York and Honolulu, Hawaii, when Toronto is 40° kilometers to the north of Honolulu?

97. **Intersecting Arcs** The pointer on a sundial is 10 centimeters in length (see figure). Find the angle through which the pointer rotates when it moves 2.2 centimeters on the scale.



$r = 6$ $2.5 = 6\theta$

Angular Speed A car is moving at a rate of 55 miles per hour, and the diameter of its wheels is 27 inches.

(a) Find the number of revolutions per minute the wheels are rotating.

(b) Find the angular speed of the wheels in radians per minute.

98. **Linear and Angular Speed** A 7.5-inch circular gear can rotate at 2200 revolutions per minute.

(a) Find the angular speed of the gear in radians per minute.

(b) Find the linear speed (in feet per minute) of one of the 20 cutting teeth as they rotate the second time out.

99. **Linear and Angular Speed** The diameter of a DVD is approximately 12 centimeters. The drive motor of the DVD player is capable of rotating between 200 and 500 revolutions per minute, depending on what track is being read.

(a) Find the angular speed of the DVD as it rotates.

(b) Find its linear speed in inches per second if it is rotating at 200 rpm.

100. **Linear and Angular Speed** A 10-inch circular gear can rotate at 2200 revolutions per minute.

(a) Find the angular speed of the gear in radians per minute.

(b) Find its linear speed in feet per second if it is rotating at 200 rpm.

101. **Linear and Angular Speed** A 10-inch circular gear can rotate at 2200 revolutions per minute.

(a) Find the angular speed of the gear in radians per minute.

(b) Find its linear speed in feet per second if it is rotating at 200 rpm.

102. **Linear and Angular Speed** A 10-inch circular gear can rotate at 2200 revolutions per minute.

(a) Find the angular speed of the gear in radians per minute.

(b) Find its linear speed in feet per second if it is rotating at 200 rpm.

103. **Linear and Angular Speed** A 10-inch circular gear can rotate at 2200 revolutions per minute.

(a) Find the angular speed of the gear in radians per minute.

(b) Find its linear speed in feet per second if it is rotating at 200 rpm.

104. **Linear and Angular Speed** A 10-inch circular gear can rotate at 2200 revolutions per minute.

(a) Find the angular speed of the gear in radians per minute.

(b) Find its linear speed in feet per second if it is rotating at 200 rpm.

105. **Linear and Angular Speed** A 10-inch circular gear can rotate at 2200 revolutions per minute.

(a) Find the angular speed of the gear in radians per minute.

(b) Find its linear speed in feet per second if it is rotating at 200 rpm.

106. **Linear and Angular Speed** A 10-inch circular gear can rotate at 2200 revolutions per minute.

(a) Find the angular speed of the gear in radians per minute.

(b) Find its linear speed in feet per second if it is rotating at 200 rpm.

107. **Linear and Angular Speed** A 10-inch circular gear can rotate at 2200 revolutions per minute.

(a) Find the angular speed of the gear in radians per minute.

(b) Find its linear speed in feet per second if it is rotating at 200 rpm.

108. **Linear and Angular Speed** A 10-inch circular gear can rotate at 2200 revolutions per minute.

(a) Find the angular speed of the gear in radians per minute.

(b) Find its linear speed in feet per second if it is rotating at 200 rpm.

109. **Linear and Angular Speed** A 10-inch circular gear can rotate at 2200 revolutions per minute.

(a) Find the angular speed of the gear in radians per minute.

(b) Find its linear speed in feet per second if it is rotating at 200 rpm.

110. **Linear and Angular Speed** A 10-inch circular gear can rotate at 2200 revolutions per minute.

(a) Find the angular speed of the gear in radians per minute.

(b) Find its linear speed in feet per second if it is rotating at 200 rpm.

111. **An angle that measures -120° lies in Quadrant III.**

112. **Find θ .** A tree trunk lies in a given angular speed. How does the speed of the tip of the trunk change if a line of greater diameter is installed on the same height?

113. **Rolling** If the radius of a circle is increasing and the magnitude of a central angle is held constant, how is the length of the intercepted arc changing? Explain your reasoning.

$11' 15' 60''$
 $3' 2' 47' 39''$
 $AL = \theta \cdot \frac{\pi}{180} \cdot 4000$

$5200 \frac{ft}{min} \cdot 2\pi = As$

$4576 \frac{ft}{min} = As$

$72229 \frac{ft}{min}$

$274560 \frac{ft}{min} = As$

125

$65\% = As \cdot 25 ft$

125

125

125

Feb 2-9:51 PM

4.3 Right Triangle Trig

SOH CAH TOA

Finding six trig ratios

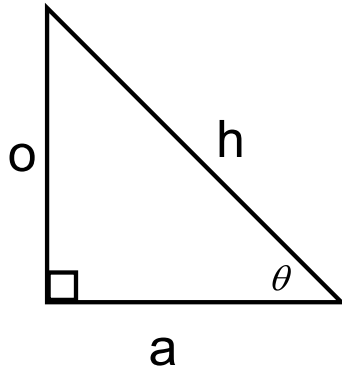
Finding theta given a ratio

Mode of your calculator

Non-common trig ratios/values

Finding theta of non-common ratios/values

Angles of elevation and depression



$$\sin \theta = \frac{o}{h}$$

$$\cos \theta = \frac{a}{h}$$

$$\tan \theta = \frac{o}{a}$$

reciprocal functions

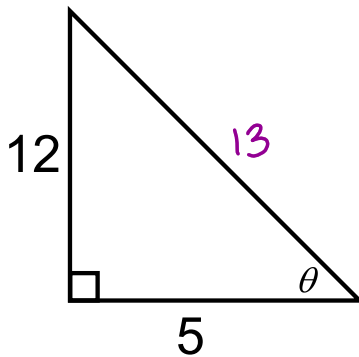
$$\csc \theta = \frac{1}{\sin \theta} = \frac{h}{o}$$

$$\sec \theta = \frac{1}{\cos \theta} = \frac{h}{a}$$

$$\cot \theta = \frac{1}{\tan \theta} = \frac{\cos \theta}{\sin \theta} = \frac{a}{o}$$

What observation can you make about $\tan \theta$?

Dec 20-8:35 AM



$$\sin \theta = \frac{12}{13}$$

$$\csc \theta = \frac{13}{12}$$

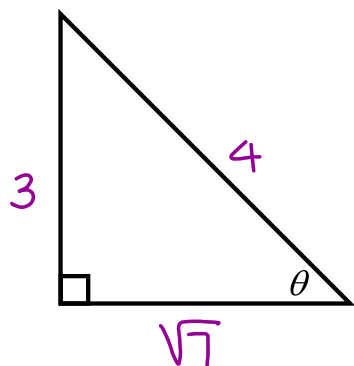
$$\cos \theta = \frac{5}{13}$$

$$\sec \theta = \frac{13}{5}$$

$$\tan \theta = \frac{12}{5}$$

$$\cot \theta = \frac{5}{12}$$

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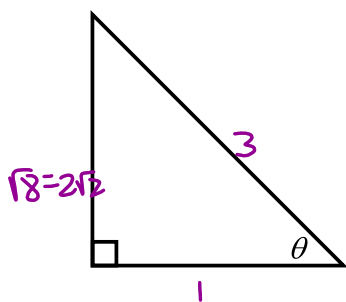


Given $\sin \theta = \frac{3}{4}$,

find the other 5 trig ratios

$$\begin{aligned} \sin \theta &= \frac{3}{4} & \csc \theta &= \frac{4}{3} \\ \cos \theta &= \frac{\sqrt{7}}{4} & \sec \theta &= \frac{4}{\sqrt{7}} \\ \tan \theta &= \frac{3}{\sqrt{7}} = \frac{3\sqrt{7}}{7} & \cot \theta &= \frac{\sqrt{7}}{3} \end{aligned}$$

Dec 20-8:59 AM



Given $\sec \theta = 3$,

find the other 5 trig ratios

$$\cos \theta = \frac{1}{3}$$

$$\begin{aligned} \sin \theta &= \frac{2\sqrt{2}}{3} & \csc \theta &= \frac{3}{2\sqrt{2}} \\ \cos \theta &= \frac{1}{3} & \sec \theta &= 3 \\ \tan \theta &= 2\sqrt{2} & \cot \theta &= \frac{1}{2\sqrt{2}} \end{aligned}$$

Remember: $\tan \theta = \frac{\sin \theta}{\cos \theta}$ and $\cot \theta = \frac{\cos \theta}{\sin \theta}$

Dec 20-8:59 AM

Now let's work backwards!

Given $\sin \theta = \frac{1}{2}$, find θ

in degrees 30°

in radians $\frac{\pi}{6}$

Dec 20-9:30 AM

Finding approximate ratios/values for those not memorized from the unit circle

we use the calculator!

$$\sin 41^\circ = .6561$$

$$\sec 32^\circ = \frac{1}{\cos 32} = 1.1792$$

$$\tan 18^\circ 31' 52'' = .3352$$

$$\cot 1.2 = \frac{1}{\tan 1.2 \text{ (in radians)}} = .3888$$

$$\cos \frac{\pi}{5} = .8090$$

$$\csc \frac{3\pi}{8} = \frac{1}{\sin \frac{3\pi}{8}} = 1.0824$$

Dec 20-9:51 AM

Now find theta when given a ratio/value

Use your calculator to find $\sin \theta = \overset{.2314}{\cancel{.3214}}$

$$0^\circ < \theta < 90^\circ \quad \sin^{-1}(.3214) \quad 0 < \theta < \frac{\pi}{2}$$

(degrees)

(radians)

$$13.38^\circ$$

$$0.23$$

Dec 20-9:57 AM

More examples:

	in radians	in degrees
$\tan \theta = 1.2563$	$.899 = .90$	51.5

$\sec \theta = 1.3514$	$.74$	42.27°
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$$\frac{1}{\cos \theta} = 1.3514$$

$$\cos \theta = \frac{1}{1.3514} \rightarrow \cos^{-1}\left(\frac{1}{1.3514}\right)$$

$$\csc \theta = 1.5826$$

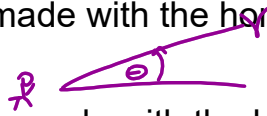
$$\sin^{-1}\left(\frac{1}{1.5826}\right)$$

$$0.684$$

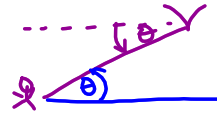
$$39.2^\circ$$

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Angle of Elevation - the angle made with the horizon when you are looking up at something



Angle of Depression - the angle made with the horizon when you are looking down at something



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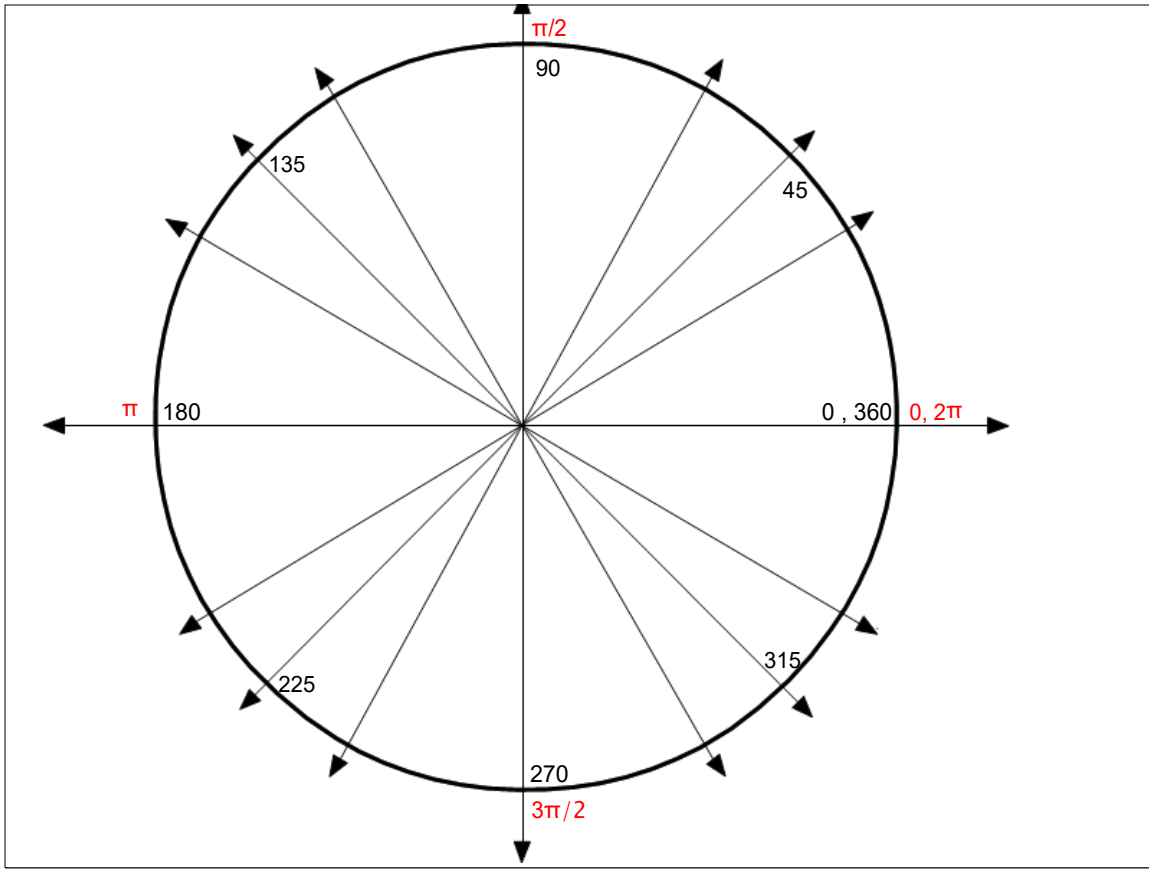
HOMWORK



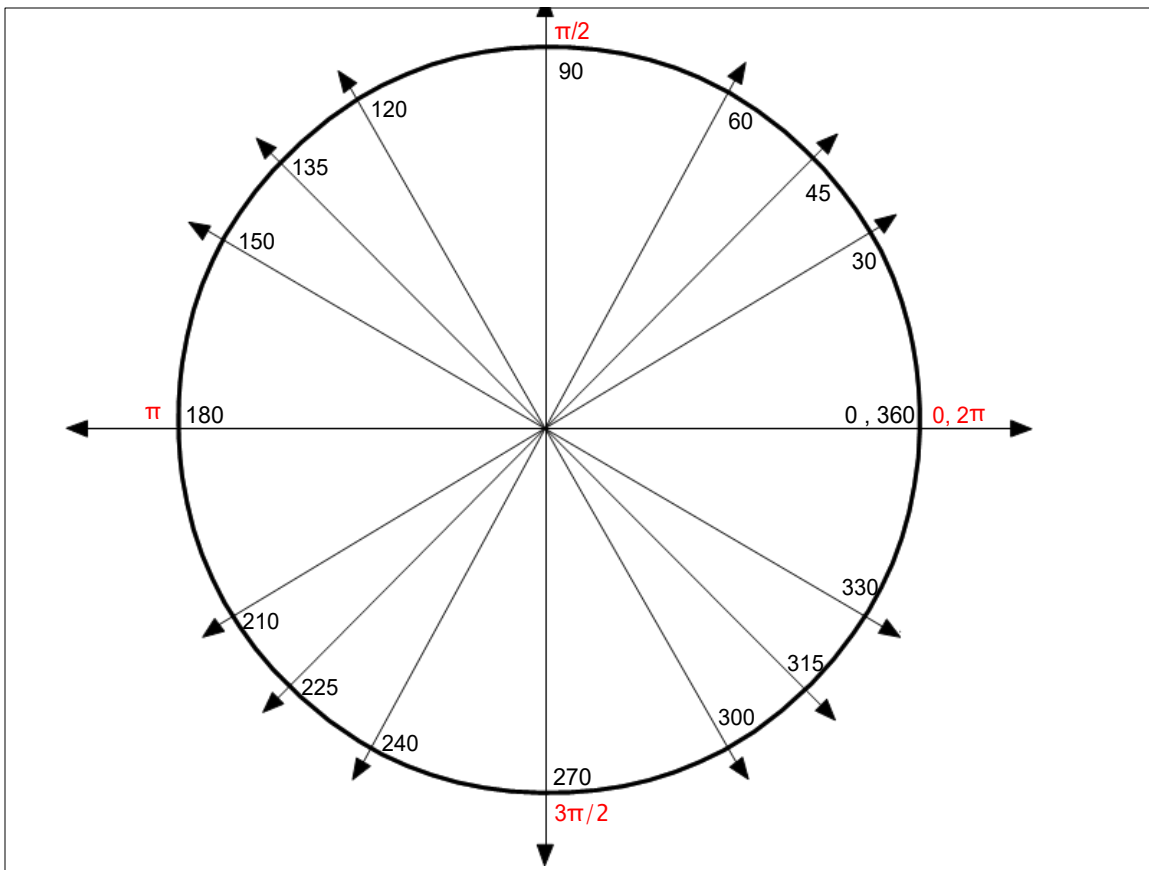
p 308 5, 9-25 odd, 51a, 53-58 all,
63, 67, 69

Workbook p 40 1-12

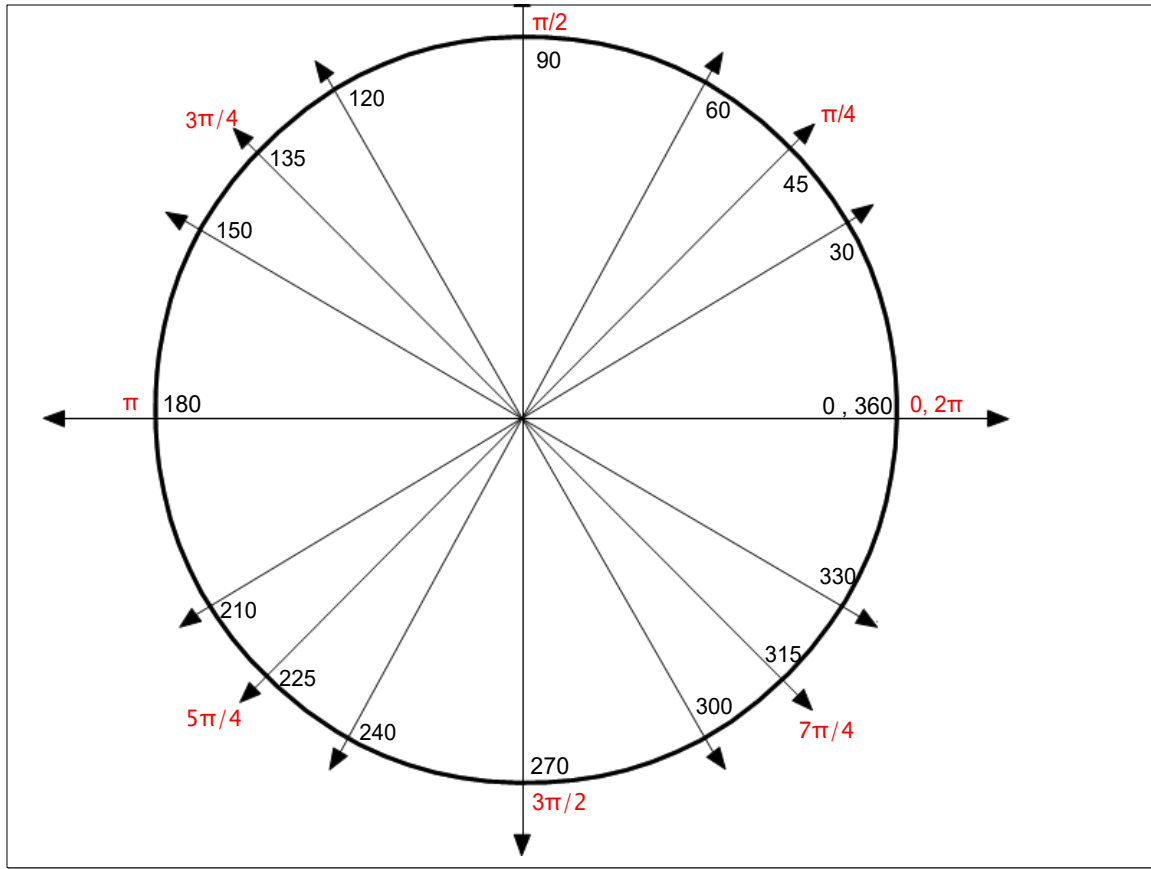
Aug 29-6:38 AM



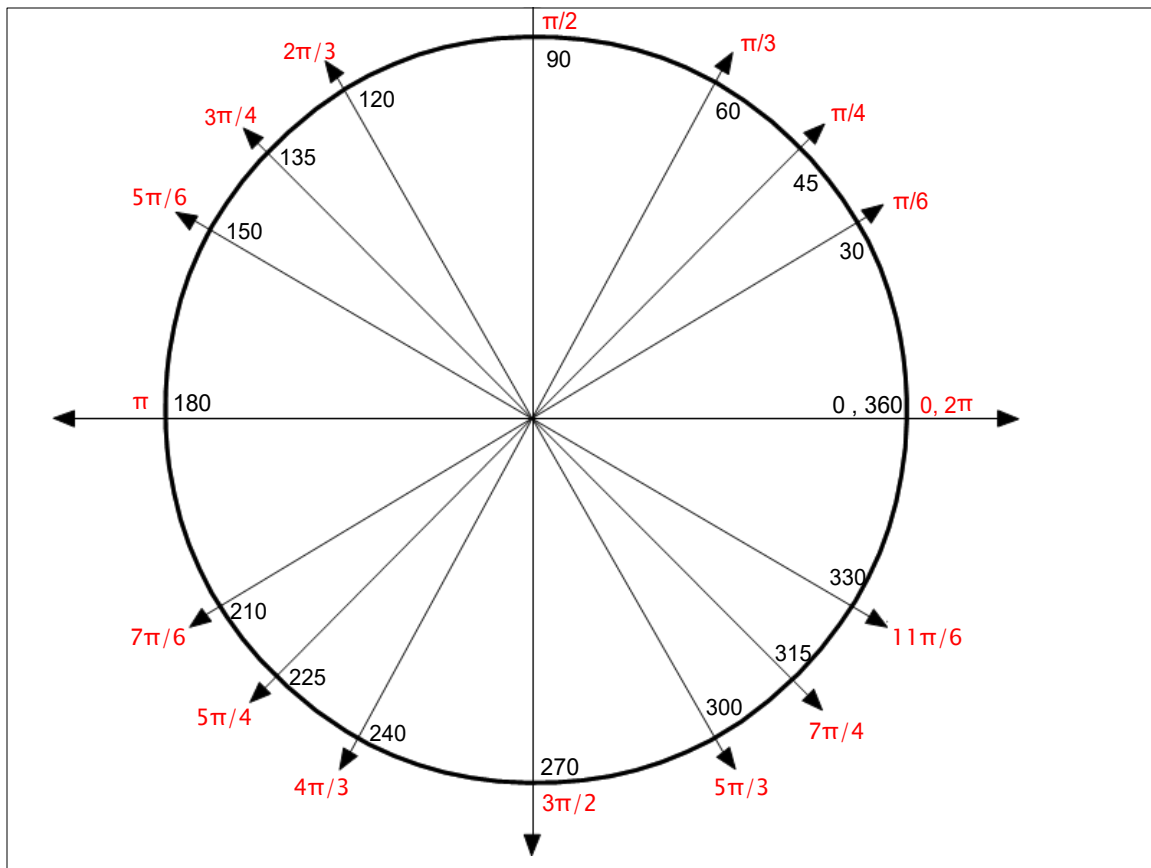
Jan 7-4:16 PM



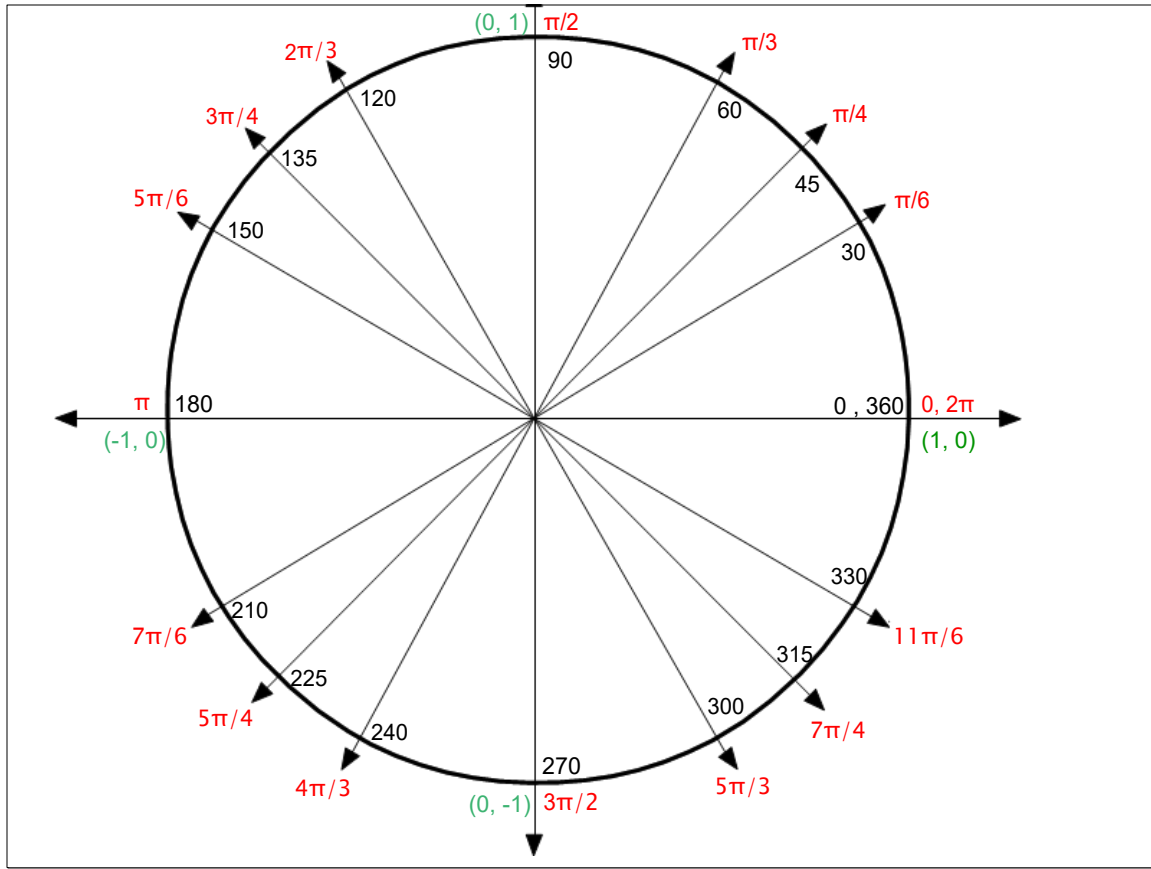
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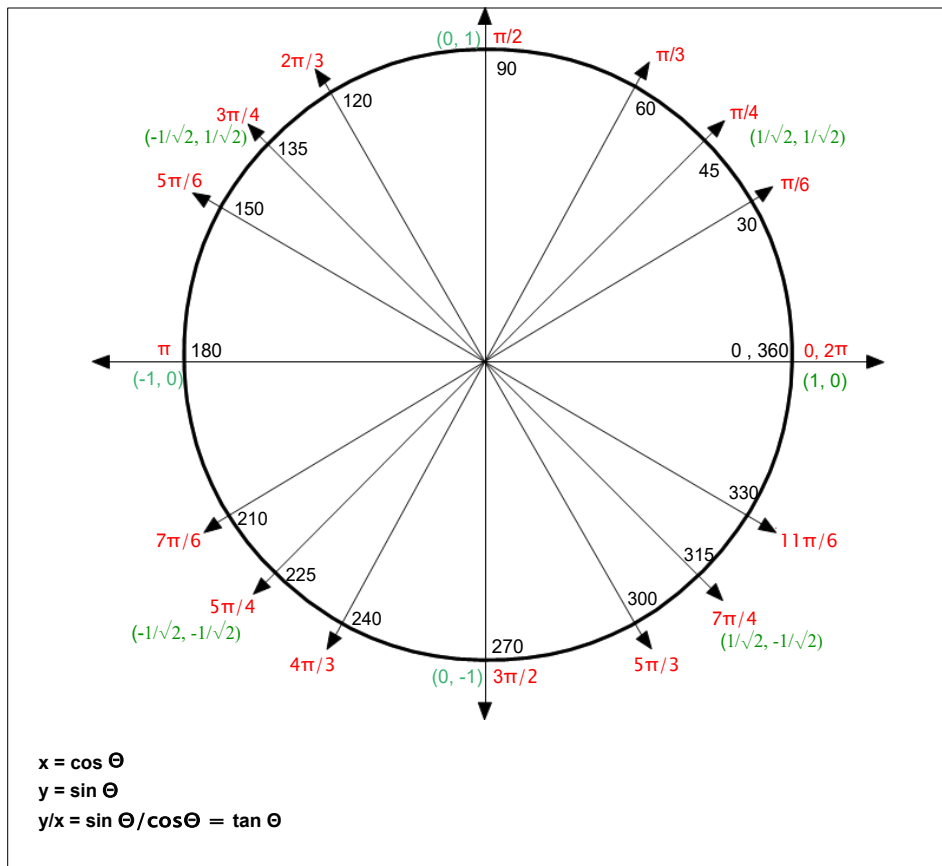
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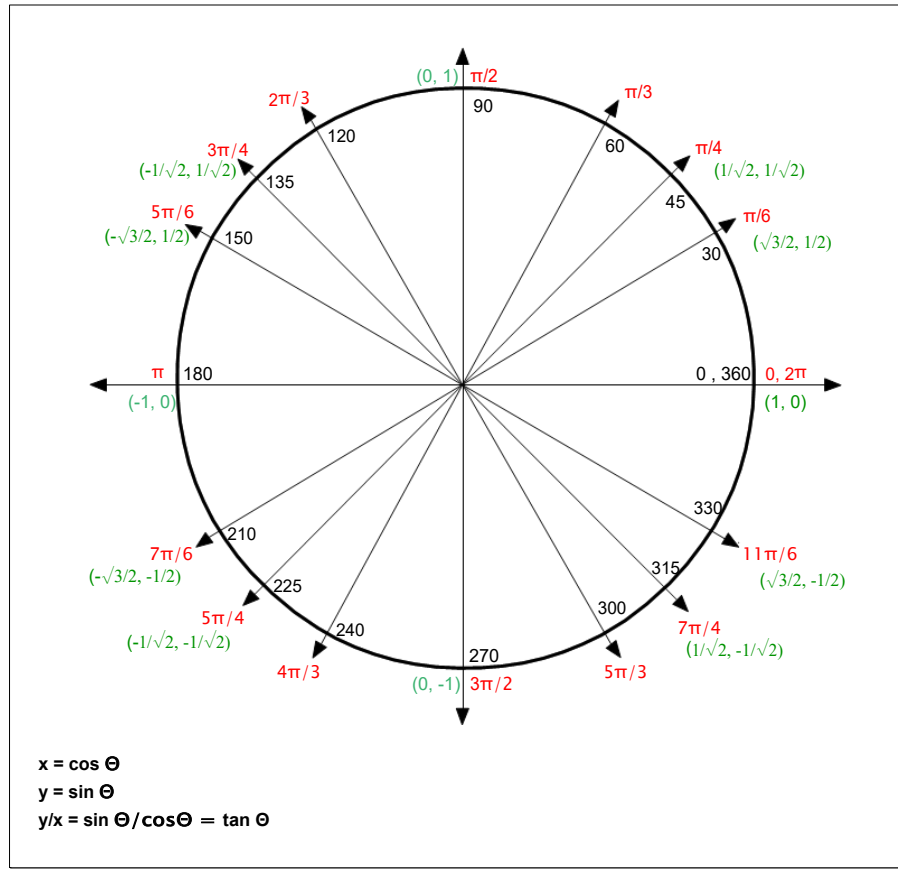


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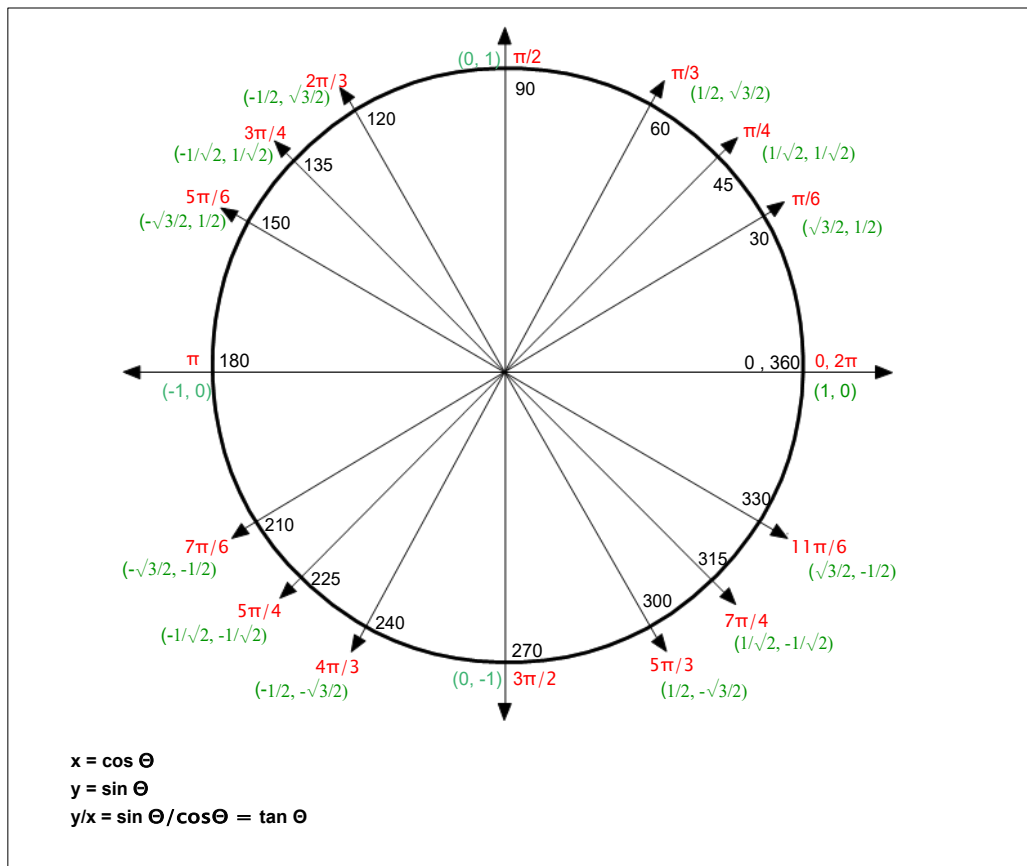


$x = \cos \theta$
 $y = \sin \theta$
 $y/x = \sin \theta / \cos \theta = \tan \theta$

Jan 7-4:20 PM



Jan 7-4:21 PM



Jan 7-4:22 PM