

5.1-5.3 Quiz Review – Check Yo' Skills/Review

Write the expression as the sine, cosine, or tangent of an angle.

1. $2\sin 100^\circ \cos 100^\circ$

$\sin 200$

2. $\frac{\tan 40^\circ - \tan 5^\circ}{1 + \tan 40^\circ \tan 5^\circ}$

$\tan 35$

Simplify the expression to a single term.

3. $(1 - 2\sin^2 \beta)^2 + 4\sin^2 \beta \cos^2 \beta$

$\cos^2 2\beta + 2\sin^2 2\beta$

4. $\frac{\tan x}{\csc^2 x} + \frac{\tan x}{\sec^2 x}$

$\tan x \sin^2 x + \tan x \cos^2 x$

$\tan x (\sin^2 x + \cos^2 x)$

$\tan x$

Prove the identity.

5. $\tan^2 x - \sin^2 x = \sin^2 x \tan^2 x$

$\frac{\sin^2 x}{\cos^2 x} - \sin^2 x$

$\frac{\sin^2 x - \sin^2 x \cos^2 x}{\cos^2 x}$

$\sin^2 x (1 - \cos^2 x) \sec^2 x$

$\sin^2 x (\sin^2 x) \cdot \sec^2 x$

$\sin^2 x \tan^2 x$

~~$\tan\left(u + \frac{3\pi}{4}\right) = \frac{\tan u - 1}{1 + \tan u}$~~

6. $2\sin \alpha \cos^3 \alpha + 2\sin^3 \alpha \cos \alpha = \sin 2\alpha$

$2\sin \alpha \cos \alpha (\cos^2 \alpha + \sin^2 \alpha)$

$2\sin \alpha \cos \alpha \cdot 1$

$= \sin 2\alpha$

8. $\frac{\cos x}{1 + \sin x} = \frac{1 - \sin x}{\cos x}$

$\frac{\cos x (1 - \sin x)}{1 + \sin x (1 - \sin x)}$

$\frac{\cos x (1 - \sin x)}{\cos^2 x}$

$\frac{1 - \sin x}{\cos x}$

Find the exact value of each expression using a sum or difference identity.

9. $\tan(-15^\circ) = \frac{\sin(30-45)}{\cos(30-45)}$

$\sin 30 \cos 45 - \cos 30 \sin 45$

$\frac{1}{2} \cdot \frac{\sqrt{2}}{2} - \frac{\sqrt{3}}{2} \cdot \frac{1}{2}$

$\frac{1 - \sqrt{3}}{2}$

$\cos 30 \cos 45 + \sin 30 \sin 45$

$\frac{\sqrt{3}}{2} \cdot \frac{1}{2} + \frac{1}{2} \cdot \frac{\sqrt{2}}{2}$

10. $\sin\left(\frac{7\pi}{12}\right) = \sin\left(\frac{3\pi}{12} + \frac{4\pi}{12}\right) = \sin\left(\frac{\pi}{4} + \frac{\pi}{3}\right)$

$\sin \frac{\pi}{4} \cos \frac{\pi}{3} + \cos \frac{\pi}{4} \sin \frac{\pi}{3}$

$\frac{1}{\sqrt{2}} \cdot \frac{1}{2} + \frac{1}{\sqrt{2}} \cdot \frac{\sqrt{3}}{2}$

$\frac{1 + \sqrt{3}}{2\sqrt{2}}$

Find all solutions in the interval $[0, 2\pi)$ without using a calculator. Give exact answers.

11. $2\cos x = 1$

$$\cos x = \frac{1}{2}$$

$$x = \frac{\pi}{3}, \frac{5\pi}{3}$$

$$x = \frac{\pi}{3} + 2k\pi, \frac{5\pi}{3} + 2k\pi$$

12. $\sin^2 x - 2\sin x - 3 = 0$

$$(\sin x - 3)(\sin x + 1) = 0$$

$$\sin x = 3 \quad \sin x = -1$$

$$\text{none} \quad x = \frac{3\pi}{2}$$

$$x = \frac{3\pi}{2} + 2k\pi$$

13. $\sin x \tan^2 x = \sin x$

$$\sin x (\tan^2 x - 1) = 0$$

$$\sin x = 0 \quad \tan x = \pm 1$$

$$x = 0, \pi \quad x = \frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}$$

$$x = k\pi, \frac{\pi}{4} + \frac{k\pi}{2}$$

Verify the identity.

14. $\cos \theta + \sin \theta \tan \theta = \sec \theta$

$$\cos \theta + \frac{\sin \theta \sin \theta}{\cos \theta}$$

$$\frac{\cos^2 \theta + \sin^2 \theta}{\cos \theta}$$

$$\frac{1}{\cos \theta}$$

$$\sec \theta$$

15. $\frac{\tan \alpha}{\sec \alpha - 1} = \frac{\sec \alpha + 1}{\tan \alpha}$

$$\frac{\tan \alpha (\sec \alpha + 1)}{(\sec \alpha - 1)(\sec \alpha + 1)}$$

$$\frac{\tan \alpha (\sec \alpha + 1)}{\tan^2 \alpha}$$

$$\frac{\sec \alpha + 1}{\tan \alpha}$$

16. $\sin(360^\circ - x) = -\sin x$

$$\sin 360 \cos x - \cos 360 \sin x$$

$$0 \cdot \cos x \quad 1 \cdot \sin x$$

$$-\sin x = -\sin x$$

17. $\frac{\csc^2 \theta - 1}{\csc^2 \theta} = \cos^2 \theta$

$$\frac{\csc^2 \theta}{\csc^2 \theta} - \frac{1}{\csc^2 \theta}$$

$$1 - \frac{\sin^2 \theta}{\cos^2 \theta}$$

$$\text{OR } \frac{\cot^2 \theta}{\csc^2 \theta}$$

$$\frac{\cot^2 \theta \sin^2 \theta}{\frac{\cos^2 \theta}{\sin^2 \theta} \cdot \sin^2 \theta} = \frac{\cos^2 \theta}{\cos^2 \theta}$$

18. $\frac{1}{1 - \cos x} + \frac{1}{1 + \cos x} = 2\csc^2 x$

$$\frac{1 + \cos x + 1 - \cos x}{1 - \cos^2 x}$$

$$\frac{2}{\sin^2 x}$$

$$2\csc^2 x$$

19. $(\cot^2 \theta + 1)(\sin^2 \theta - 1) = -\cot^2 \theta$

$$\csc^2 \theta (-\cos^2 \theta)$$

$$\frac{1}{\sin^2 \theta} (-\cos^2 \theta)$$

$$-\cot^2 \theta$$